A Theory of Socially Responsible Investment *

Martin Oehmke† Marcus Opp‡

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Abstract

We characterize necessary conditions for socially responsible investors to impact firm behavior in a setting in which firm production generates social costs and is subject to financing constraints. Impact requires a broad mandate, in that socially responsible investors need to internalize social costs irrespective of whether they are investors in a given firm. Impact is optimally achieved by enabling a scale increase for clean production. Socially responsible and financial investors are complementary: jointly they can achieve higher welfare than either investor type alone. When socially responsible capital is scarce, it should be allocated based on a social profitability index (SPI). This micro-founded ESG metric captures not only a firm’s social status quo but also the counterfactual social costs produced in the absence of socially responsible investors.

Keywords: Socially responsible investing, ESG, SPI, capital allocation, sustainable investment, social ratings.

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†London School of Economics and CEPR, e-mail: m.oehmke@lse.ac.uk.
‡Stockholm School of Economics, e-mail: marcus.opp@hhs.se.
In recent years, the question of the social responsibility of business, famously raised by Friedman (1970), has re-emerged in the context of the spectacular rise of socially responsible investment (SRI). Assets under management in socially responsible funds have grown manifold, and many traditional investors consider augmenting their asset allocation with environmental, social, and governance (ESG) scores (Pastor et al., 2019, Pedersen et al., 2019). From an asset management perspective, this trend raises immediate questions about the financial performance of such investments (Hong and Kacperczyk, 2009, Chava, 2014, Barber et al., 2018). However, if socially responsible investing is to generate real impact, it must affect firms’ production decisions. This raises additional, fundamental questions: Under which conditions can socially responsible investors impact firm behavior? And how should scarce socially responsible capital be allocated across firms?

Answering these questions requires taking a corporate finance view of socially responsible investment. To this end, we incorporate socially responsible investors and the choice between clean and dirty production into an otherwise standard model of corporate financing with agency frictions, building on Holmström and Tirole (1997). The model’s main results are driven by the interaction of financing constraints (leading to underinvestment in socially desirable clean production) and negative production externalities (which can lead to overinvestment in socially undesirable dirty production).

We find that socially responsible investors can indeed push firms to adopt clean production. They optimally do so by raising a firm’s financing capacity under clean production beyond the amount that purely profit-motivated investors would provide. The resulting increase in clean production raises welfare, even compared to the scenario where all capital is held by socially responsible investors. However, increasing clean production beyond the scale that profit-motivated investors would fund is only possible if socially responsible make financial losses. Therefore, a necessary condition for socially responsible

\footnote{For example, the Global Sustainable Investment Alliance (2018) reports sustainable investing assets of $30.7tn at the beginning of 2018, an increase of 34\% relative to two years prior.}
investors to break even, in social terms, on their impact investments is that they follow a broad mandate, in the sense that they internalize social costs generated by firms regardless of whether they are investors in these firms. When faced with an investment decision across many heterogeneous firms, scarce socially responsible capital should be allocated according to a social profitability index (SPI). One key feature of this micro-founded ESG metric is that avoided social costs (in addition to their actual level) are relevant for ranking investments. Hence, investments in “sin” industries are not necessarily inconsistent with the mandate of being socially responsible.

We develop these results in a parsimonious model, initially focusing on the investment decision of a single firm. The firm is owned by an entrepreneur with limited wealth, who has access to two constant-returns-to-scale production technologies, dirty and clean. Dirty production has a higher per-unit financial return, but entails significant social costs. Clean production is financially less attractive but socially preferable, because it generates lower (although not necessarily zero) social costs. Production under either technology requires the entrepreneur to exert unobservable effort, so that not all cash flows are pledgeable to outside investors. The firm can raise funding from (up to) two types of outside investors. Financial investors behave competitively and, as their name suggests, care solely about financial returns. Socially responsible investors also care about financial returns, but, in addition, they satisfy two conditions that, as our analysis reveals, are necessary for impact. First, they care unconditionally about external social costs generated by the firm (i.e., irrespective of whether they are investors in the firm). Second, they act in a coordinated fashion, so that they internalize the effect of their investments on production decisions. Socially responsible investors in our model are therefore most easily interpreted as a large (e.g., sovereign wealth) fund.

As a benchmark, we initially consider a setting in which only financial investors are present. Because of the entrepreneur’s moral hazard problem, the amount of outside financing and, hence, the firm’s scale of production are limited. Since the dirty production
technology is financially more attractive, financial investors offer better financing terms for dirty production, enabling a larger production scale than under the clean technology. As a result, the entrepreneur may adopt the socially inefficient dirty production technology, even if she partially internalizes the associated externalities due to an intrinsic preference for clean production.

We then analyze whether and how socially responsible investors can address this social inefficiency. We show that the optimal way to achieve impact (i.e., induce a change in the firm’s production technology) is to relax financing constraints for clean production, thereby enabling additional value creation. One way the firm can implement the resulting financing agreement by issuing two bonds, a green bond purchased by socially responsible investors and a regular bond purchased by financial investors. However, because financial investors are not willing to provide this scale on their own, the extra financing must involve a financial loss to socially responsible investors. Therefore, the green bond is issued at a premium, consistent with evidence in Baker et al. (2018) and Zerbib (2019).

Our results highlight a complementarity between socially responsible and financial investors. Because of this complementarity, welfare (which, in our model, is equivalent to the total scale of clean production) is generally higher when both types of investors are present. The complementarity between socially responsible and financial investors arises from the respective comparative advantage of each investor type. Compared to socially responsible investors, financial investors are more aggressive in providing financing as they view a project (under either technology) as more profitable, thereby alleviating the underinvestment problem that results from agency frictions. However, because of their disregard for externalities, financial investors facilitate the adoption of the socially inefficient dirty technology, creating scope for socially responsible investors to guide the firm’s choice of technology. In doing so, the threat of dirty production relaxes the participation constraint of socially responsible investors and, thereby, acts like a quasi asset to the entrepreneur that allows the financing of the clean technology. Therefore, the presence of
financial investors is instrumental to unlocking the additional capital socially responsible investors provide for the clean technology.

Our analysis identifies three necessary conditions for this complementarity to arise. First, socially responsible investors need to follow a broad mandate. This means that they must care unconditionally about external social costs of production, whether or not they are investors in the firm that produces them. If socially responsible investors follow a narrow mandate, in that they only care about social costs generated by their own investment, they cannot impact production decisions, since dirty production will then simply be financed by financial investors. Second, the clean technology must be subject to financing constraints, so that additional clean scale is socially valuable. Third, socially responsible capital needs to be in sufficient supply to be able to discipline the threat of dirty production. If this is not the case, dirty production is not merely an off-equilibrium threat, but occurs in equilibrium.

While socially responsible capital has seen substantial growth over the last few years, it is likely that such capital remains scarce relative to financial capital that simply chases financial returns. This raises the question of how scarce socially responsible capital is invested most efficiently. Which firms should impact investors target? A multi-firm extension of our model yields a micro-founded investment criterion for scarce socially responsible capital, the *Social Profitability Index* (SPI).

Similar to the profitability index, the SPI measures “bang for buck”— i.e., value created for socially responsible investors per unit of socially responsible capital consumed. However, unlike the conventional profitability index, the SPI not only reflects the (social) return of the project that is being funded, but also the counterfactual social costs that a firm would have generated in the absence of investment by socially responsible investors. For example, investment metrics for socially responsible investors should include estimates of carbon emissions that can be avoided if the firm adopts a cleaner production technology. Because avoided externalities matter, it can be efficient for socially respon-
sible investors to invest in firms that, in an absolute sense, generate a high level of social costs even under clean production. Accordingly, investments in sin industries (see Hong and Kacperczyk (2009)) can be consistent with socially responsible investing. In contrast, it is efficient to not invest in firms that are already committed to clean production (e.g., because, intrinsically, the entrepreneur cares sufficiently about the environment), because clean production will occur regardless of investment by socially responsible investors.

The SPI also rationalizes why environmental, social, and governance issues are often bundled into one ESG score. In our model, a connection between these distinct aspects of corporate behavior arises naturally, because the severity of the manager’s agency problem (a proxy for governance) determines the financing constraints the firm faces with respect to both financial and socially responsible investors. The SPI reflects these financing constraints because they interact with the externalities (environmental and social) generated by the firm. Therefore, the SPI incorporates all three ESG elements.

Throughout the paper, we abstract away from government intervention. One way to interpret our results is therefore as characterizing the extent to which the market can fix problems of social cost before the government imposes regulation or Pigouvian taxes. Another interpretation is that our analysis concerns those social costs that remain after the government has intervened. For example, informational frictions and political economy constraints may make it difficult for governments to apply Pigouvian taxes or ban dirty production. However, even if government intervention is possible, our analysis reveals that text-book regulation, in the form of Pigouvian taxes or a ban on dirty production, may result in lower welfare than the allocation achieved via co-investment by financial and socially responsible investors. While Pigouvian taxes or bans on dirty production would certainly ensure the adoption of the clean technology (even when financing is provided by financial investors only), such regulation also eliminates the threat of dirty production.

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2 Examples of social costs for which government intervention is likely to be particularly difficult include those where the relevant externality is global in nature, as is the case for carbon emissions or systemic externalities caused by large financial institutions.
which is necessary to unlock additional capital by socially responsible investors. The broader point is that regulation that targets one source of inefficiency (externalities) but does not address the other (financing constraints) has limited effectiveness in our setting.

**Related Literature.** Despite the growing interest in socially responsible investing (see, e.g., Landier and Nair, 2009), the theory literature on this topic is still relatively small. In a pioneering contribution, Heinkel et al. (2001) show that firms that are excluded by socially responsible investors suffer a reduction in risk-sharing among their investor base. The resulting increase in the cost of capital can induce firms to clean up their activities.\(^3\) Hart and Zingales (2017) characterize the objective of a firm with prosocial investors, who dislike social costs if they feel directly responsible for them. They argue that firms should maximize shareholder welfare instead of shareholder value. Socially responsible investors in our model are similar to prosocial investors, with the important difference that they care about externalities regardless of whether they are directly responsible for them. Chowdhry et al. (2018) study the financing of a firm that cannot commit pursuing social goals. A common theme with our paper is that the firm can monetize the socially-minded investors’ social preference. However, their analysis focuses on how socially-minded investors can blunt a firm’s profit motive (in the spirit of Glaeser and Shleifer, 2001) thereby allowing the firm to commit to emphasize social goals. In contrast, we focus on the ability of socially responsible investors to impact firms by relaxing financial constraints for clean production. Roth (2019) contrasts impact investing with grants or donations, highlighting the ability of investors to withdraw capital as a potential advantage over grants. While in our model socially responsible investors must necessarily make a financial loss, Gollier and Pouget (2014) provide a model in which a large activist investor can generate positive abnormal returns by reforming firms and then selling them back to the market. Finally, our analysis highlights that, in order

\(^3\)However, as Davies and Van Wesep (2018) point out, divestment can also have unintended consequences, for example, by inducing firms to prioritize short-term profit at the expense of long-term value.
to have impact, socially responsible investors need to act in a coordinated fashion. Morgan and Tumlinson (forthcoming) provide a more detailed analysis of potential free-rider problems among investors and show how those can be overcome.

1 Model Setup

Our modeling framework aims to uncover the role of socially responsible investing in a setting in which production externalities interact with financing constraints. It builds on the canonical model of corporate financing in the presence of agency frictions laid out in Holmström and Tirole (1997) and Tirole (2006). The main innovation is that the firm has access to two different production technologies, one of them “clean” (i.e., associated with low social costs) and the other “dirty” (i.e., associated with larger social costs). To focus on the role that socially responsible investors can play in alleviating distortions, we abstract away from government intervention for most of the paper. In Section 4.2, we discuss the effects of standard regulatory policies, such as Pigouvian taxes or banning the dirty production technology.

The entrepreneur, production, and moral hazard. Our setting considers a risk-neutral entrepreneur who is protected by limited liability and endowed with initial liquid assets of $A$. The entrepreneur has access to two production technologies $\tau \in \{C, D\}$, each with constant returns to scale. The technologies are identical in terms of revenue generation. Denoting firm scale (capital) by $K$, the firm generates positive cash flow of $RK$ with probability $p$ (conditional on effort by the entrepreneur, as discussed below)

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4 The two technologies can therefore be interpreted as those available to the firm after government intervention has taken place. Because government intervention is usually subject to informational and political economy constraints, it seems reasonable that the social costs of production cannot be dealt with by the government alone, creating a potential role for socially responsible investors. Alternatively, our analysis can be interpreted as establishing what market forces (in the form of socially responsible investors) can achieve before government intervention takes place.

5 In Section 4.1, we discuss robustness of our results to $N > 2$ technologies and decreasing returns to scale.
and zero otherwise.

Where the technologies differ is with respect to the required ex-ante investment and the social costs they generate. In particular, the dirty technology $D$ generates a non-pecuniary negative externality of $\phi_D > 0$ per unit of scale and requires a per-unit upfront investment of $k_D$. The clean technology results in a lower per-unit social cost $0 < \phi_C < \phi_D$, but requires a higher per-unit upfront investment of $k_C > k_D$. The entrepreneur internalizes a fraction $\gamma^E \in [0, 1)$ of social costs, capturing potential intrinsic motives not to cause social harm.

To generate a meaningful trade-off in the choice of technologies, we assume that the ranking of the two technologies differs depending on whether it is based on financial or social value. Denoting the per-unit financial value by $\pi_r := pR - k_r$ and the per-unit social value (welfare) by $v_r := \pi_r - \phi_r$, we assume that the dirty technology has higher financial value, $\pi_D > \pi_C$, but clean production generates higher social value, $v_C > 0 > v_D$.\footnote{Once we allow for $N$ technologies (see Section 4.1), we show how our results readily extend to cases where the dirtiest technology may no longer be the profit-maximizing technology. The case where the clean technology also maximizes profits is uninteresting for our analysis of socially responsible investment, since even purely profit-motivated capital would ensure clean production in this case.}

The final inequality implies that the social value of the dirty production technologies is negative, meaning that the externalities caused by dirty production outweigh its financial value. The assumption that the dirty production technology has negative social value is not necessary for our results, but it simplifies the exposition because it implies that, from a social perspective, the dirty technology should never be adopted.

As in Holmström and Tirole (1997), the entrepreneur is subject to an agency problem. Whereas the choice of production technology is assumed to be observable (and, hence, contractible) effort is assumed to be unobservable (and, therefore, not contractible). Under each technology, the investment pays off with probability $p$ only if the entrepreneur exerts effort ($a = 1$). The payoff probability is reduced to $p - \Delta p$ when the entrepreneur shirks ($a = 0$), where $p > \Delta p > 0$. Shirking yields a per-unit non-pecuniary benefit of $B$ to the entrepreneur, for a total private benefit of $BK$. A standard result (which we
will show below) is that this agency friction reduces the firm’s unit pledgeable income by 
\( \xi := p \frac{B}{\Delta p} \), the per-unit agency cost. A high value of \( \xi \) can be interpreted as an indicator of poor governance, such as large private benefits or weak performance measurement.

We make the following assumption on the per-unit agency cost:

**Assumption 1** For each technology \( \tau \), the agency cost per unit of capital \( \xi := p \frac{B}{\Delta p} \) satisfies

\[
\pi_\tau < \xi < pR - \frac{p}{\Delta p} \pi_\tau.
\]

(1)

This assumption states that the moral hazard problem, as characterized by the agency cost per unit of capital \( \xi \), is neither too weak nor too severe. The first inequality implies a finite production scale. The second inequality is a sufficient condition that rules out equilibrium shirking and ensures feasibility of outside financing. To streamline notation, \( \pi \) and \( v \) are defined conditional on the relevant case, in which the entrepreneur exerts effort (as usual, shirking is an off-equilibrium action).

**Outside investors and securities.** The entrepreneur can raise financing from (up to) two types of risk-neutral outside investors \( i \in \{F, SR\} \), financial investors and socially responsible investors. Both investor types care about expected cash flows, but only socially responsible investors internalize social costs of production (i.e., \( \gamma^{SR} > 0 \), whereas \( \gamma^{F} = 0 \)).\(^7\)\(^8\) Regardless of whether the entrepreneur raises financing from both investor types or just one, it is without loss of generality to restrict attention to financing arrangements in which the entrepreneur issues securities that pay a total amount of \( X := X^F + X^{SR} \) upon project success and 0 otherwise, where \( X^F \) and \( X^{SR} \) denote the payments promised to financial and socially responsible investors, respectively. Given that the firm has no resources in the low state, this security can be interpreted as debt

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\(^7\) The assumption that at least some investors internalize social costs is consistent with evidence in Riedl and Smeets (2017) and Bonnefon et al. (2019).

\(^8\) In our model, financial investors literally do not care about social costs. However, an alternative setting, in which financial investors do care about social costs but do not act on them because of a free-rider problem, would yield equivalent results.
or equity. The entrepreneur’s utility can then be written as a function of the investment scale $K$, the total promised repayment $X$, the effort decision $a$, upfront consumption by the entrepreneur $c$, and the technology choice $\tau \in \{C, D\}$,

$$U^E(K, X, \tau, c, a) = p(RK - X) - (A - c) - \gamma^E \phi_\tau K + \mathbb{1}_{a=0}[BK - \Delta p(RK - X)].$$ \hspace{1cm} (U^E)$$

The first two terms of this expression, $p(RK - X) - (A - c)$, represent the project’s net financial payoff to the entrepreneur under high effort, where $A - c$ can be interpreted as the upfront co-investment made by the entrepreneur. The third term, $\gamma^E \phi_\tau K$, measures the social cost internalized by the entrepreneur. The final term, $BK - \Delta p(RK - X)$, captures the incremental payoff conditional on shirking ($a = 0$). Exerting effort is incentive compatible if and only if $U^E(K, X, \tau, c, 1) \geq U^E(K, X, \tau, c, 0)$, which limits the total amount $X$ that the entrepreneur can promise to repay to outside investors to

$$X \leq \left( R - \frac{B}{\Delta p} \right) K.$$ \hspace{1cm} (IC)

Per unit of scale, the entrepreneur’s pledgeable income is therefore given by $pR - \xi$.

The resource constraint at date 0 implies that capital expenditures, $Kk_\tau$, must equal the total investments made by the entrepreneur and outside investors,

$$Kk_\tau = A - c + I^F + I^{SR},$$ \hspace{1cm} (2)

where $I^F$ and $I^{SR}$ represent the investments of financial and socially responsible investors, respectively.

We impose two conditions on the behavior of socially responsible investors. As we will show later, both of these conditions are necessary for socially responsible investors to have impact.
**Condition 1 (Broad Mandate)**  *Socially responsible investors are affected by externalities $\gamma^{SR} \phi r K$ regardless of whether they invest in the firm.*

**Condition 2 (Coordination)**  *Socially responsible investors allocate their capital in a coordinated fashion.*

Effectively, these conditions imply that socially responsible investors care unconditionally about externalities and are willing to act on them. Coordination is necessary because socially responsible investors need to take into account that their investment affects the social cost generated by the firm. This condition is naturally satisfied if socially responsible capital is directed by one large fund, such as the Norwegian sovereign wealth fund. Another interpretation is that socially responsible investors are dispersed, but have found a way to overcome the free-rider problem that would usually arise.$^9$

Under Conditions 1 and 2 the respective utility functions of outside investors, given an incentive-compatible financing arrangement, can be written as

\[
U^F = pX^F - I^F, \tag{U^F}
\]

\[
U^{SR} = pX^{SR} - I^{SR} - \gamma^{SR} \phi r K, \tag{U^{SR}}
\]

where $\gamma^{SR}$ captures the degree to which socially responsible investors internalize the social costs generated by the firm. The sum $\gamma^E + \gamma^{SR} \in (0, 1]$ represents the fraction of total externalities that are taken into account by investors and the entrepreneur. The case $\gamma^E + \gamma^{SR} < 1$ can be interpreted in two ways. First, it may represent the case where some externalities (e.g., those imposed on future generations) are simply not taken into account by agents in the model. Second, it may capture, in reduced form, the effect of imperfect coordination among small investors. In the extreme case of $\gamma^{SR} = 0$, the free rider problem is so severe that socially responsible investors effectively act like financial

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$^9$ One such example is the establishment of the Poseidon Principles, an initiative by eleven major to promote green shipping, see Nauman (2019). Dimson et al. (2019) empirically document coordinated engagements by large investors.
investors.

2 The Effect of Socially Responsible Investment

In this section, we investigate whether and how socially responsible investors can impact a single firm’s investment choice, assuming that socially responsible capital is abundant relative to the funding needs of the firm. Our subsequent multi-firm setting in Section 3 analyzes how scarce socially responsible capital should be optimally allocated across firms. In Section 2.1, we first solve a benchmark case of firm financing without socially responsible investors. This benchmark shows that, when investors care exclusively about financial returns, the dirty technology may be chosen even when the entrepreneur has some concern for the higher social cost generated by dirty production (i.e., when $\gamma^E > 0$). In Section 2.2, we add socially responsible investors to the model and characterize conditions under which their presence has impact, in the sense that it changes the firm’s production decision.

2.1 Benchmark: Financing from Financial Investors Only

The setting in which the entrepreneur can borrow exclusively from competitive financial investors corresponds to the special case $I^{SR} = X^{SR} = 0$. Then, the entrepreneur’s objective is to choose a financing arrangement (consisting of scale $K \geq 0$, repayment $X^F \in [0, R]$, upfront consumption by the entrepreneur $c \geq 0$, and technology choice $\tau \in \{C, D\}$) that maximizes the entrepreneur’s utility $U^E$ subject to the entrepreneur’s IC constraint and financial investors’ IR constraint, $U^F \geq 0$.

As a preliminary step, it is useful analyze the financing arrangement that maximizes scale for a given technology $\tau$. Following standard arguments (see Tirole, 2006), this agreement requires the entrepreneur to co-invest all her wealth (i.e., $c = 0$) and that $U^E \geq 0$.

As discussed below, given competitive investors, maximizing scale is indeed optimal if the technology generates positive surplus from the entrepreneur’s perspective.
the entrepreneur’s IC constraint as well as the financial investors’ IR constraint bind. 
The binding IC constraint ensures that the firm optimally leverages its initial resources 
A, whereas the binding IR constraint is a consequence of competition among financial 
investors.

When all outside financing is raised from financial investors, the maximum firm scale 
under production technology τ is then given by

\[ K^F = \frac{A}{\xi - \pi_\tau}. \]  (3)

This expression shows that the entrepreneur can scale her initial assets A by a factor 
that depends on the agency cost per unit of investment, \( \xi := \frac{p R}{\Delta p} \), and the financial 
return under technology τ, \( \pi_\tau \). As \( \xi > \pi_D \) (see Assumption 1), the maximum investment 
scale is finite under either technology. The key observation from Equation (3) is that the 
maximum scale that the entrepreneur can finance from financial investors is larger under 
dirty than under clean production, \( K^F_D > K^F_C \), since dirty production generates larger 
financial value, \( \pi_D > \pi_C \), and financial investors only care about financial returns.

The following lemma highlights that the entrepreneur’s technology choice \( \bar{\tau} \) is then 
driven by a trade-off between achieving scale and her concern for externalities. Of course, 
if the entrepreneur completely disregards externalities (\( \gamma^E = 0 \)), no trade-off arises and 
the entrepreneur always chooses dirty production to maximize scale.

Lemma 1 (Benchmark: Financial Investors Only) When only financial investors 
are present, the entrepreneur chooses

\[ \bar{\tau} = \arg \max_{\tau} (\xi - \gamma^E \phi_\tau)K^F_\tau. \]  (4)

The firm operates at the maximum scale that allows financial investors to break even,
The entrepreneur’s utility is given by

\[ \bar{U}^E = (\xi - \gamma^E \phi^E)K^F - A. \] (5)

According to Lemma 1, the entrepreneur chooses the technology that maximizes her payoff, which is given by the product of the per-unit payoff to the entrepreneur (agency rent net of internalized social cost) and the maximum scale under technology \( \tau \) (given by Equation (4)). Maximum scale is optimal because, under the equilibrium technology \( \bar{\tau} \), the project generates positive surplus for the entrepreneur and financial investors. It follows that the entrepreneur adopts the dirty technology whenever

\[ (\xi - \gamma^F \phi^F)K^F_D > (\xi - \gamma^F \phi^C)K^F_C. \] (6)

Given that the maximum scale is larger under the dirty technology, \( K^F_D > K^F_C \), this condition is satisfied whenever the entrepreneur’s concern for externalities \( \gamma^E \) lies below a strictly positive cutoff \( \bar{\gamma}^E \).\(^{11}\)

**Corollary 1 (Financial Investors Can Induce Dirty Production)** When only financial investors are present, the entrepreneur adopts the dirty production technology when \( \gamma^E < \bar{\gamma}^E := \frac{\xi(\pi_D - \pi_C)}{\phi_D(\xi - \pi_C) - \phi_C(\xi - \pi_D)}. \)

Overall, this benchmark case shows that there is a potential role for socially responsible investors to steer the entrepreneur towards the clean production technology as long as \( \gamma^E < \bar{\gamma}^E \).

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\(^{11}\)Given the funding terms offered by financial investors, the entrepreneur may adopt the dirty technology even if, judging by project payoffs alone, she prefers the clean technology (i.e., when \( \pi_C - \gamma^F \phi_C > \pi_D - \gamma^E \phi_D \)). This occurs on the (non-empty) interval \( (\tilde{\gamma}^E, \bar{\gamma}^E) \), where \( \tilde{\gamma}^E := \frac{\pi_D - \pi_C}{\phi_D - \phi_C} \). These entrepreneurs are “corrupted” by the financing conditions offered by financial investors.
2.2 Equilibrium with Socially Responsible Investors

We now analyze whether and how the financing arrangement and the resulting technology choice are altered when socially responsible investors are present. Because the entrepreneur could still raise financing exclusively from financial investors, the utility she receives under the financing arrangement with financial investors only, $\bar{U}^E$, now takes the role of an outside option to the entrepreneur.

2.2.1 Optimal Financial Contract with Socially Responsible Investors

Due to the broad mandate Condition 1, socially responsible investors are affected by the social costs of production regardless of whether they have a financial stake in the firm. In particular, if socially responsible investors remain passive, their (reservation) utility is given by

$$\bar{U}^{SR} = -\gamma^{SR} \phi_{\tau} K^F_{\tau} < 0,$$

which reflects the social costs generated when the entrepreneur chooses the optimal production technology $\tau$ and scale $K^F_{\tau}$ (see Lemma 1) when raising financing from financial investors only.

To improve their payoff relative to this outside option, socially responsible investors can engage with the entrepreneur. Because socially responsible investors act in a coordinated fashion, they make a take-it-or-leave-it contract offer that specifies the technology $\tau$, scale $K$ as well as the required financial investments and payoffs for all investors and the entrepreneur. This contract solves the following maximization problem:

**Problem 1 (Maximization Problem Faced by Socially Responsible Investors)**

$$\max_{I^F, I^{SR}, X^{SR}, X^F, K, \phi, \gamma^{SR} \phi_{\tau}} p X^{SR} - I^{SR} - \gamma^{SR} \phi_{\tau} K$$
subject to the entrepreneur’s IR constraint:

\[ U^E (K, X^{SR} + X^F, \tau, c, 1) \geq \bar{U}^E, \]  

\text{(IRE)}

as well as the entrepreneur’s IC constraint, the resource constraint (2), the financial investors’ IR constraint \( U^F \geq 0 \), and the non-negativity constraints \( K \geq 0, c \geq 0 \).

The key difference relative to the benchmark case is that financing and technology are now chosen to maximize socially responsible investors’ utility subject to the constraint that the entrepreneur is weakly better off than under the outside option of raising financing exclusively from financial investors, \( \bar{U}^E \). Note that this formulation permits the possibility of compensating the entrepreneur with sufficiently high upfront consumption (\( c > 0 \)) in return for smaller scale \( K \), possibly even shutting down production completely (as in the typical Coasian solution, see Coase, 1960). However, because (at a minimum) the clean production technology generates positive joint surplus for the entrepreneur and socially responsible investors, the optimal financing arrangement rewards the entrepreneur with larger scale (relative to what could be funded by financial investors alone) rather than upfront consumption.

**Proposition 1 (Financing in the Presence of Socially Responsible Investors)**

Let \( \hat{\hat{\tau}} := \pi_\tau - (\gamma^E + \gamma^{SR}) \phi_\tau \geq v_\tau := \pi_\tau - \phi_\tau \) denote the joint surplus, per unit of scale, accruing to all investors and the entrepreneur. Then, in any optimal financing arrangement, production is characterized by

\[ \hat{\hat{\tau}} = \arg \max_{\tau} \frac{\hat{\hat{\tau}}}{\xi - \gamma^E \phi_\tau}, \]  

\[ \hat{\hat{K}} = \frac{\xi - \gamma^E \phi_\hat{\hat{\tau}}}{\xi - \gamma^F \phi_{\hat{\hat{\tau}}}} K^F. \]

The entrepreneur consumes no resources upfront, \( \hat{c} = 0 \). The total date-0 investment (by both investors) is \( \hat{I} = \hat{\hat{K}} k_{\hat{\hat{\tau}}} - A \) and the total payout (to both investors) satisfies
\( \hat{X} = \left( R - \frac{B}{\Delta p} \right) \hat{K} \). The set of optimal co-investment arrangements can be obtained by tracing out the cash-flow share accruing to socially responsible investors \( \lambda \in [0, 1] \) and setting \( \hat{X}^{\text{SR}} = \lambda \hat{X}, \hat{X}^{F} = (1 - \lambda) \hat{X}, \hat{I}^{F} = p\hat{X}^{F} \) and \( \hat{I}^{\text{SR}} = \hat{I} - \hat{I}^{F} \). The utility of socially responsible investors is given by:

\[
\hat{U}^{\text{SR}} = (\pi_{\hat{r}} - \xi) \hat{K} + A - \gamma^{\text{SR}} \phi_{\hat{r}} \hat{K}.
\] (11)

Proposition 1 contains the main theoretical results of the paper. It shows that when both types of investors are present, the optimal choice of technology maximizes total joint surplus, which is governed by the joint surplus that is created per unit of capital, \( \hat{v}_{\tau} \), and a term, \( \frac{1}{\xi - \gamma^{E} \phi_{\hat{r}}} \), that reflects the optimal scale \( \hat{K} \) (see Equation (10)). An immediate implication is that if the entrepreneur and socially responsible investors jointly internalize all externalities, \( \gamma^{E} + \gamma^{\text{SR}} = 1 \), production will always be clean, since, in this case, joint surplus \( \hat{v}_{\tau} \) coincides with social welfare \( v_{\tau} \).

Moreover, Proposition 1 shows that the optimal financing arrangement rewards the entrepreneur entirely with scale, in the sense that the optimal capital stock \( \hat{K} \) is chosen so that the entrepreneur obtains the same utility as under her outside option \( \bar{U}^{E} \). Intuitively, any upfront consumption by the entrepreneur is suboptimal in the presence of a moral hazard problem that gives rise to capital rationing and, consequently, underinvestment.

**Implementation.** While the optimal financing arrangement uniquely pins down the production side (i.e., technology choice and scale), there exists a continuum of co-investment arrangements between financial and socially responsible investors that solve Problem 1. Intuitively, any increase in the cash flow share accruing to financial investors translates at competitive terms into higher upfront investment by financial investors, \( \hat{I}^{F} \). Because also the entrepreneur remains at her reservation utility \( \bar{U}^{E} \), the payoff to socially

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\(^{12}\) Since \( v_{D} < 0 \), the dirty technology would never be chosen. Note that, once we allow for multiple technologies with \( v_{\tau} \geq 0 \) (see Section 4.1), technologies are not ranked exclusively according to the per-unit surplus because, in this case, maximum scale matters as well.
responsible investors as well as aggregate surplus remain unchanged.

There are two particularly intuitive ways in which the optimal financing arrangement characterized in Proposition 1 can be implemented.\footnote{Under both implementations, the security targeted at socially responsible investors is issued at a premium in the primary market (see Corollary 4 below), ensuring that only socially responsible investors have an incentive to purchase this security.}

**Corollary 2** The following securities implement the optimal financing agreement:

1. **Green bond and regular bond:** The entrepreneur issues two bonds with respective face values $\hat{X}^F$ and $\hat{X}^{SR}$ at respective prices $\hat{I}^F$ and $\hat{I}^{SR}$. The green bond contains a technology-choice covenant specifying technology $\hat{\tau}$.

2. **Dual-class share structure:** The entrepreneur issues voting and non-voting shares, where shares with voting rights yield an issuance amount of $\hat{I}^{SR}$ in return for control rights and a fraction $\lambda$ of dividends. The remaining proceeds $\hat{I}^F$ are obtained in return for non-voting shares with a claim on a fraction $1 - \lambda$ of dividends.

**2.2.2 Impact**

To highlight the economic mechanism behind Proposition 1, this section provides a more detailed investigation of the case in which socially responsible investors have impact, where we define impact as an induced change in the firm’s production decision, through a switch in technology from $\bar{\tau} = D$ to $\hat{\tau} = C$ and/or a change in scale.\footnote{If investment by socially responsible investors does not result in a change in production technology compared to the benchmark case (i.e., $\hat{\tau} = \bar{\tau}$), there is no impact and we obtain the same level of investment and utility for all agents in the economy as in the benchmark case. This (less interesting) situation occurs either if the entrepreneur adopts the clean production technology even in the absence of investment by socially responsible investors, or if the entrepreneur adopts the dirty technology irrespective of whether socially responsible investors provide funding.}

**Corollary 3** Socially responsible investors have impact if and only if $\gamma^E < \bar{\gamma}^E$ and $\gamma^{SR} > \bar{\gamma}^{SR}$, where the threshold $\bar{\gamma}^{SR}$ is a decreasing function of $\gamma^E$.

**Complementarity between Financial and Social Capital.** The following proposition highlights that when this condition for impact is satisfied, the equilibrium features
a complementarity between financial and socially responsible investors.

**Proposition 2 (Financial and Social Capital Are Complementary)** Suppose that $\gamma^E < \gamma^E$ and $\gamma^{SR} > \gamma^{SR}$, then financial capital and socially responsible capital act as complements in that the equilibrium clean scale with both investor types, $\hat{K}$, is larger than the maximum clean scale that can be financed in an economy with only one of the two investor types,

$$\hat{K} > K^F_C > K^{SR}_C.$$  \hspace{1cm} (12)

Proposition 2 is a consequence of the interaction of financing constraints and externalities. Financing constraints imply that, conditional on choosing the clean technology, there is underinvestment (recall that $v_C > 0$ and there are constant returns to scale, so that the socially optimal scale of clean production is infinite). If only financial investors are present or, equivalently, if they hold all the capital in the economy (as in the benchmark case presented in Lemma 1), the maximum clean scale is given by $K^F_C = \frac{A}{\xi - \pi_C}$, which exceeds the corresponding break-even scale in the opposite case when only socially responsible investors are present, $K^{SR}_C = \frac{A}{\xi - \pi_C + \gamma^{SR} \phi_C}$. Hence, financial investors in isolation are better positioned to alleviate the financing constraints with respect to the clean technology, precisely because they disregard externalities and, therefore, perceive each scale unit of the clean technology as more valuable (by $\gamma^{SR} \phi_C$).\textsuperscript{15} In this context, it is important to note that the objective of socially responsible investors (see $U^{SR}$) differs from the maximization of social surplus $v_C K$ even if $\gamma^{SR} = 1$, because socially responsible investors do not internalize rents that accrue to the entrepreneur.

The key feature of Proposition 2 is that the equilibrium scale in the presence of both investor types, $\hat{K}$, strictly exceeds the financing that is available with only one of the investor types. This complementarity arises because financial investors are willing to finance an even larger scale under the dirty production technology, $K^D_F > K^F_C$, thereby pro-

\textsuperscript{15} Only in the case in which the clean technology generates no externalities are the break-even scales offered by each investor type in isolation identical.
viding the entrepreneur with the outside option of adopting dirty production. The resulting pollution threat relaxes the participation constraint of socially responsible investors, through its effect on their reservation utility, which is given by $\bar{U}^{SR} = -\gamma^{SR} \phi_D K_D^F$. This reduction in reservation utility unlocks additional financing from socially responsible investors, relative to the clean scale that is possible when raising financing from financial investors, $\bar{K} > K_C^F$. The optimum scale $\bar{K}$ is chosen by socially responsible investors to just induce the entrepreneur to switch to the clean production technology.\(^ {16}\)

In sum, Proposition 2 implies that social surplus is higher when both financial and socially responsible investors deploy capital, relative to the case in which all capital is allocated by either financial or socially responsible investors. Intuitively, the counterfactual social cost $\gamma^{SR} \phi_D K_D^F$, which is enabled by the presence of financial investors, acts as a quasi asset to the firm, thereby generating additional financing capacity from socially responsible investors.\(^ {17}\)

**The cost of impact.** Even though socially responsible investors only invest if doing so increases their utility relative to the case in which they remain passive,

$$\Delta U^{SR} := \hat{U}^{SR} - \bar{U}^{SR} = \hat{v}_C \bar{K} - \hat{v}_D K_D^F \geq 0, \quad (13)$$

they do not break even in financial terms on their impact investment.

**Corollary 4 (Socially Responsible Investors Make a Financial Loss)** Impact (a switch from $\bar{\tau} = D$ to $\hat{\tau} = C$) requires that socially responsible investors make a financial

\(^{16}\)When the entrepreneur does not internalize any of the social costs of production ($\gamma^E = 0$), this switch from dirty to clean requires that the production scale under the clean technology is the same as the scale that financial investors would fund under the dirty technology (i.e., $\bar{K} = K_D^F > K_C^F$). If $\gamma^E > 0$, it is sufficient for socially responsible investors to partially make up for lost scale, because the entrepreneur internalizes part of the reduction in social costs that results from the switch to clean production (i.e., $K_D^F > \bar{K} > K_C^F$).

\(^{17}\)This interpretation can be formalized as follows. The break-even scale when financing is raised form both financial and socially responsible investors can be written as $\frac{A + \hat{A}}{1 - \pi_C + \gamma^{SR} \phi_C}$. The quasi asset $\hat{A} := \gamma^{SR} \phi_D K_D^F > 0$ enters the maximum scale in exactly the same way as the entrepreneur’s financial assets $A$. 

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loss. That is, in any optimal financing arrangement as characterized in Proposition 1,

\[ p\hat{X}^{SR} < \hat{I}^{SR}. \]  \hspace{1cm} (14)

Intuitively, to induce a change from dirty to clean production, socially responsible
investors need to enable a scale for the clean technology greater than the clean scale
offered by competitive financial investors in isolation. Because financial investors just
break even at that scale, socially responsible investors must make a financial loss on any
additional scale they finance.\(^{18}\) Empirically, Corollary 4 therefore predicts that impact
funds must have a negative alpha or, equivalently, that funds generating weakly positive
alpha cannot generate (real) impact.

Our model also predicts that the financial loss for socially responsible investors,
\( p\hat{X}^{SR} - \hat{I}^{SR} \), occurs at the time when the firm seeks to finance investment in the primary
market, consistent with evidence on the at-issue pricing of green bonds in Baker et al.
(2018) and Zerbib (2019). However, if socially responsible investors were to sell their cash
flow stake \( \hat{X}^{SR} \) to financial investors after the firm has financed the clean technology,
our model does not predict a price premium for the “green” security in the secondary
market (i.e., in the secondary market, the security would be fairly priced at \( p\hat{X}^{SR} \)).\(^{19}\)

**Necessary conditions for impact.** The analysis above reveals why Conditions 1
and 2 are both necessary for socially responsible investors to have impact. To see the
necessity of the broad mandate, suppose first that Condition 1 is violated and that
socially responsible investors follow a narrow mandate, in that they only care about social
costs that are a direct consequence their own investments. Because, under the narrow
mandate, socially responsible investors ignore the social costs of firms that are financed

\(^{18}\) Socially responsible investors are nevertheless willing to provide financing because their financial loss,
\( p\hat{X}^{SR} - \hat{I}^{SR} \), is outweighed by the utility gain resulting from reduced social costs, \( \gamma^{SR} \left( \phi_{D}K_{D}^{F} - \phi_{C}\hat{K} \right) \).

\(^{19}\) Intuitively, in our static model, control (or a technology covenant) only matters once, at the time
of initial investment. In a more general, dynamic setting, control could matter multiple times (e.g.,
whenever investment technologies are chosen).
by financial investors, the threat of dirty production does not relax their participation constraint. Hence, the key force that generates the additional financing capacity for clean production (see Proposition 2) is absent and, therefore, no impact can be achieved.\textsuperscript{20}

Next suppose that socially responsible investors are infinitesimal and uncoordinated, so that Condition 2 is violated. Then, due to the resulting free-rider problem, each individual investor takes social costs generated by the firm as given and, therefore, behaves as if $\gamma^{SR} = 0$. No impact can be achieved because socially responsible investors behave like financial investors.

Finally, a third necessary condition for impact is that socially responsible capital is available in sufficient amounts to ensure adoption of the clean production technology. When this is not the case, the presence of financial capital can induce firms to adopt the dirty production technology, leading to a social loss. We discuss this case in Section 3, where we consider an economy with multiple firms and limited socially responsible capital. This analysis will shed further light on how the composition of investor capital (and not just the aggregate amount) matters for welfare.

3 The Social Profitability Index

Based on the framework presented above, we now derive a micro-founded investment criterion to guide scarce socially responsible capital. To do so, we extend the single-firm analysis presented in Section 2 to a multi-firm setting with limited socially responsible capital.

Let $\kappa$ be the aggregate amount of socially responsible capital (we continue to assume that financial capital is abundant) and consider an economy with a continuum of infinitesimal firms grouped into distinct firm types.\textsuperscript{21} Firms that belong to the same

\textsuperscript{20}In Section 4.3, we will discuss risk aversion and risk-premia effects of exclusion under a narrow mandate.

\textsuperscript{21}The assumption that firms are infinitesimally small is made only to rule out well-known difficulties that can arise when ranking investment opportunities of discrete size.
firm type \( j \) are identical in terms of all relevant parameters of the model, whereas firms belonging to distinct types differ according to at least one dimension (with Assumption 1 satisfied for all types). Let \( \mu(j) \) denote the distribution function of firm types, then the aggregate social cost in the absence of socially responsible investors is given by

\[
\int_{\gamma_j^E < \bar{\gamma}_j^E} \phi_{D,j} K_{D,j}^E d\mu(j) + \int_{\gamma_j^E \geq \bar{\gamma}_j^E} \phi_{C,j} K_{C,j}^E d\mu(j).
\]

(15)

The first term of this expression captures the social cost generated by firms that, in the absence of socially responsible investors, choose the dirty technology \( (\gamma_j^E < \bar{\gamma}_j^E) \), whereas the second term captures firm types run by entrepreneurs that have enough concern for external social costs that they choose the clean technology even in absence of socially responsible investors \( (\gamma_j^E \geq \bar{\gamma}_j^E) \).

Given this aggregate social cost, how should socially responsible investors allocate their limited capital? One direct implication of Proposition 1 is that any investment in firm types with \( \gamma_j^E \geq \bar{\gamma}_j^E \) cannot be optimal as these firms adopt the clean technology even when raising financing from financial investors only. For the remaining firm types, the payoff to socially responsible investors from “reforming” a firm of type \( j \) is given by:

\[
\Delta U_j^{SR} = (\pi_{C,j} - \xi_j) \hat{K}_j + A_j + \gamma^{SR} \left[ \phi_{D,j} K_{D,j}^E - \phi_{C,j} \hat{K}_j \right].
\]

(16)

The first two terms of this expression capture the total financial payoff to socially responsible investors, net of the agency cost that is necessary to incentivize the entrepreneur. The third term captures the (internalized) change in social cost that results from inducing a firm of type \( j \) to adopt the clean production technology.

Given limited capital, socially responsible investors are generally not able to reform all firms. They should therefore prioritize investments in firm types that maximize the impact per dollar invested. This is achieved by ranking firms according to a variation on the classic profitability index, the social profitability index (SPI). The SPI divides
the change in payoffs to socially responsible investors, $\Delta U_{j}^{SR}$, by the amount socially responsible investors need to invest to impact the firm’s behavior, $I_{j}^{SR}$.\footnote{The change in the payoff to socially responsible investors, $\Delta U_{j}^{SR}$, is the same across all financing agreements characterized in Proposition 1. Absent other constraints, it is therefore optimal for socially responsible investors to choose the minimum co-investment that implements clean production.}

$$SPI_{j} = \mathbb{1}_{\gamma_{j}^{E} < \bar{\gamma}_{j}^{E}} \frac{\Delta U_{j}^{SR}}{I_{j}^{SR}},$$

(17)

**Proposition 3 (The Social Profitability Index (SPI))**  
Socially responsible investors should rank firms according to the social profitability index, $SPI_{j}$. There exists a threshold $SPI^{*}(\kappa) \geq 0$ such that socially responsible investors with scarce capital $\kappa$ should invest in all firms for which $SPI_{j} \geq SPI^{*}(\kappa)$.

According to Proposition 3, it is optimal to invest in firms ranked by the SPI until no funds are left, which happens at the cutoff $SPI^{*}(\kappa)$. Social capital is scarce if and only if the amount $\kappa$ is not sufficient to fund all firm types with $SPI_{j} > 0$. The SPI links the attractiveness of an investment by socially responsible investors to underlying parameters of the model, thereby shedding light on the types of investments that socially responsible investors should prioritize.

**Proposition 4 (SPI Comparative Statics)**  
As long as $\gamma_{j}^{E} < \bar{\gamma}_{j}^{E}$, the SPI is increasing in the avoided social cost, $\Delta \phi := \phi_{D} - \phi_{C}$, and the entrepreneur’s concern for social cost, $\gamma_{j}^{E}$, and decreasing in the financial cost associated with switching to the clean technology, $\Delta \pi := k_{C} - k_{D}$.

According to Proposition 4, socially responsible investors should prioritize in firms for which avoided social cost is high is high, as reflected in the difference in social costs under the clean and the dirty technology, $\Delta \phi$. Because the SPI reflects the relative social cost, it can be optimal for socially responsible investors to invest in firms that generate significant social costs provided that these firms would have caused even larger
social costs in the absence of engagement by socially responsible investors. Of course, the potential to avoid social costs, as summarized by the $\Delta \phi_j$, has to be traded off against the associated financial costs, as measured by the resulting reduction in profits $\Delta \pi_j$.

Another implication is that, as long as $\gamma_j^E < \gamma_j^E$, firms with more socially minded entrepreneurs should be prioritized, because they require a smaller investment from socially responsible investors to be convinced to reform. However, as soon as the entrepreneur internalizes enough of the externalities, so that she chooses the clean technology even if financed by financial investors (i.e., $\gamma_j^E \geq \gamma_j^E$), the SPI drops discontinuously to zero. Socially responsible investors should not invest in these firms.

To obtain a closed-form expression for the SPI, it is useful to consider the special case of $\gamma^E = 0$ and $\gamma^{SR} = 1$. Moreover, while strictly speaking it is optimal to minimize socially responsible investors’ investment by selling all cash flow rights to financial investors, suppose that socially responsible investors need to receive a fraction $\lambda_j$ of a firm’s cash flow rights. This minimum cash-flow stake pins down $I_j^{SR}$. The assumption of a required cash-flow stake for socially responsible investors can be justified on two grounds. First, it seems natural that socially responsible investors cannot rely purely on the “warm-glow” utility that results from reducing social costs, but require a certain amount of financial payoffs alongside non-pecuniary payoffs. Second, the minimum cash flow share $\lambda_j$ can be interpreted as a reduced form representation of the control rights that are necessary to implement ensure that firm $j$ implements the clean technology. Given these assumptions, the SPI takes the following simple expression,

$$\text{SPI}_j = \frac{\Delta \phi_j - \Delta \pi_j}{\Delta \pi_j + \lambda_j (p_j R_j - \xi_j)}.$$  \hspace{1cm} (18)

This expression not only transparently reveals the comparative statics described in

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\[23\] This could be the case because the entrepreneur cannot commit to the adoption of the clean technology. In this case, a cash-flow stake for socially responsible investors and blunt the entrepreneur’s profit motive (see Chowdhry et al., 2018) or may allow socially responsible investors to enforce appropriate technology adoption, for example, via voting rights.
Proposition 4, but also yields an additional insight regarding the role of the agency cost. Equation (18) shows that the SPI is increasing in the per-unit agency cost $\xi$. This may seem counterintuitive, because higher agency costs imply that, per unit of scale, a larger fraction of cash flows needs to go to the entrepreneur. However, higher agency costs also reduce the entrepreneur’s outside option, because it lowers the scale she could finance from financial investors under the dirty technology. This second effect dominates, making it cheaper for socially responsible investors to reform the firm.

To conclude this section, we briefly revisit the complementarity result given in Proposition 2 in a setting with limited socially responsible capital. The welfare change relative to the case without socially responsible investors, $\Delta \Omega$, results purely from the set of reformed firms: firms for which $\gamma^E_j < \tilde{\gamma}^E_j$ and $SPI_j \geq SPI^*(\kappa)$. We can therefore write the change in welfare as

$$\Delta \Omega = \int_{j|\gamma^E_j < \tilde{\gamma}^E_j \& SPI_j \geq SPI^*(\kappa)} \left( v_{C,j} \hat{K}_j - v_{D,j} K^F_{D,j} \right) d\mu(j). \quad (19)$$

Clearly, if socially responsible capital is abundant, the results of Proposition 2 still apply: Welfare is strictly higher in an economy with both types of investors than in an economy where all capital is held exclusively by either financial or socially responsible investors. In contrast, when socially responsible capital is scarce there is a trade-off. On the one hand, the set of reformed firms contributes towards higher welfare, as before. On the other hand, the set of unreformed “dirty” firms exhibit overinvestment in the dirty technology due to the presence of competitive financial capital without regard for externalities. This trade-off implies that the right balance between socially responsible and financial capital is important for a complementarity between the two types of capital to arise.
4 Discussion

4.1 Generalizing the production technology

In our baseline model, we considered the choice between two constant-returns-to-scale production technologies with identical cash flows and agency rents. Moreover, we focused on the case, in which externalities of production are negative for all production technologies. As we show in this section, these assumptions can be relaxed relatively straightforwardly. In particular, Proposition 1 generalizes to multiple technologies and social goods. Moreover, even when the production technology exhibits decreasing returns to scale, it remains optimal to reward the entrepreneur with additional scale as long as financing frictions for the clean technology are significant.

Many technologies and social goods. Let us first retain the assumption of constant returns to scale, but generalize all other dimensions of the available production technologies. In particular, suppose that the entrepreneur has access to $N$ production technologies characterized by technology-specific cash flow, cost, and moral hazard parameters $R_\tau$, $k_\tau$, $p_\tau$, $\Delta p_\tau$, and $B_\tau$. Moreover, assume that, in contrast to the baseline model, the technology-specific social cost parameter $\phi_\tau$ can be negative, in which case the technology generates a positive externality (a social good).

In analogy to the baseline model, we can then define, for each technology $\tau \in \{1, ..., N\}$, the financial value $\pi_\tau$, the agency rent $\xi_\tau$, and the maximum scale available from financial investors $K^F_\tau$, maintaining the assumption that $\xi_\tau > \pi_\tau$ for all $\tau$, so that the maximum scale of production is finite. A straightforward extension of Lemma 1 then implies that, in the absence of investment by socially responsible investors, the entrepreneur chooses the technology $\bar{\tau}$ such that:

$$\bar{\tau} = \arg \max_{\tau} \frac{\pi_\tau - \gamma^F \phi_\tau}{\xi_\tau - \pi_\tau}. \quad (20)$$
Equation (20) shows that even with \( N \) general technologies, the entrepreneur’s choice of technology is essentially the same as in Lemma 1, with the exception that the agency cost \( \xi_\tau \) is now project specific and that the externality can be positive (when \( \phi_\tau < 0 \)). Moreover, Equation (20) clarifies the entrepreneur’s relevant outside option in the presence of \( N \) technologies: In particular, adopting any production technology dirtier than \( \bar{\tau} \) is not a credible threat.

The induced technology choice in the presence of socially responsible investors \( \hat{\tau} \) and the associated capital stock \( \hat{K} \) are given by

\[
\hat{\tau} = \arg \max_{\tau} \frac{\hat{v}_\tau}{\xi_\tau - \gamma E\phi_\tau}, \quad (21)
\]

\[
\hat{K} = \begin{cases} 
\xi_\tau - \gamma E\phi_\tau K^F \hat{\tau}, & \hat{v}_\tau > 0 \\
0 & \hat{v}_\tau \leq 0
\end{cases} \quad (22)
\]

These expressions mirror Proposition 1, except that technology choice and scale in the presence of socially responsible investors now also depend on the technology-specific severity of the agency problem \( \xi_\tau \). Ceteris paribus, a smaller agency problem makes it more likely that a technology is adopted, both in the presence of financial investors only (Equation (20)) and when there is co-investment by socially responsible investors (Equation (21)).

This more general technology specification yields insights about cases that we previously excluded. First, it is possible that for some industries the cleanest technology also maximizes financial value (e.g., because of demand by socially responsible consumers). In this case, there is no trade-off between doing good and doing well and, hence, socially responsible investors play no role. Second, the dirty technology may be the socially optimal technology when cleaner technologies are too expensive. Also in this case, there is no role for socially responsible investors. Finally, it is possible that, for some industries, any feasible technology \( \tau \) yields negative social value (i.e., \( \hat{v}_\tau < 0 \)). In this case, the socially
optimal scale is zero and the entrepreneur is optimally rewarded with a transfer \( \hat{c} > 0 \) to shut down production.

**Decreasing returns to scale.** We now consider the case in which the two production technologies \( \tau \in \{ C, D \} \) exhibit decreasing returns to scale. In particular, suppose that the marginal financial value \( \pi_\tau(K) \) is strictly decreasing in \( K \). Then, the first-best scale \( K^{FB}_C \) under the (socially efficient) clean technology is characterized by the first-order condition

\[
\pi_C(K^{FB}_C) = \phi_C.
\] (23)

Now consider the scenario in which technology \( D \) is chosen in the absence of socially responsible investors, with an associated scale of \( K^{F}_D \). Moreover, for ease of exposition, focus on the case \( \gamma_E + \gamma_{SR} = 1 \), so that socially responsible investors have incentives to implement first-best scale. The optimal financing agreement that socially responsible investors offer to induce the entrepreneur to switch to the clean technology then comprises three cases.

1. If the financing constraints generated by the agency problem are severe, so that the maximum clean scale under the benchmark financing agreement with financial investors lies below a cutoff \( \bar{K} \), i.e., \( K^{F}_C \leq \bar{K} < K^{FB}_C \), the optimal agreement offered by socially responsible investors rewards the entrepreneur exclusively through an increase in scale (rather than upfront consumption), as in Proposition 1. Even with socially responsible investors, the resulting clean scale, \( \hat{K} \), is smaller than first-best scale (i.e., \( \hat{K} \leq K^{FB}_C \)), with equality when \( K^{F}_C = \bar{K} \).

2. If the financing constraints generated by the agency problem are intermediate, i.e., \( \bar{K} < K^{F}_C \leq K^{FB}_C \), the optimal agreement specifies the first-best scale, \( \hat{K} = K^{FB}_C \). In this case, it is efficient to increase clean scale up to the first-best level but no further, since scale above and beyond \( K^{FB}_C \) would reduce joint surplus. Inducing
the entrepreneur to switch technologies solely through an increase in scale would require a production scale exceeds the first-best level $K_{CB}^{FB}$. It is therefore optimal to partially compensate the entrepreneur through an upfront consumption transfer.

3. If financing constraints are mild, so that $K_{CB}^{F} > K_{CB}^{FB}$, then financial investors alone would provide funding above and beyond the first-best scale of the clean production technology (note that this case can only occur if $\phi_{C} > 0$). In this case, the optimal financing agreement with socially responsible investors ensures that the clean production technology is run at the first-best scale, $K = K < K_{CB}^{F}$. To induce the entrepreneur to switch to the clean technology at a lower scale than financial investors would finance, the agreement includes an upfront consumption transfer to the entrepreneur.

The above reasoning shows that, as long as financing constraints are significant (as in cases 1 and 2), the main insights of the baseline analysis continue to hold even under decreasing returns to scale: Socially responsible investors optimally achieve impact by relaxing financing constraints and increasing scale for the clean technology. Only when financing constraints are mild (or absent), socially responsible investors optimally achieve impact by reducing firm investment. Note that this latter case resembles a Coasian solution in a setting without financing constraints. For example, a downstream fishery might pay an upstream factory to reduce production (see Coase, 1960).

### 4.2 Regulation

Our analysis so far focused on what socially responsible investors can achieve in the absence of regulation (or when regulation is not optimally set). While the design of optimal regulation is beyond the scope of this paper, our analysis reveals that standard policy

\[\text{Note that in cases 2 and 3, the agreement would need to explicitly limit the amount of firm investment (and not just specify the technology). Otherwise, the entrepreneur would find it privately optimal to convert the upfront consumption into additional firm investment.}\]
interventions (e.g., an outright ban of dirty production or a Pigouvian tax) generally cannot restore efficiency in the presence of financing constraints.\footnote{See Hoffmann et al. (2017) for an analysis of optimal regulation in a related setting with financial constraints.} In fact, in some situations such interventions can lead to worse outcomes than no intervention at all.

**Banning the dirty technology.** Suppose regulators could simply ban the dirty production technology. With clean production as the only feasible technology, this intervention certainly ensures that the entrepreneur adopts the socially efficient production technology. However, in the context of our baseline model, the scale of production under the clean technology would be strictly lower, equal to $K^F_C$, compared to the case when dirty production is allowed but socially responsible investors ensure that the entrepreneur adopts the clean production technology with scale $\hat{K} > K^F_C$. Intuitively, the key ingredient for the additional financing capacity from socially responsible investors is the (credible) threat of dirty production (see Proposition 2). Banning dirty production eliminates this threat, so that socially responsible investors are unwilling to extend financing above and beyond the scale offered by financial investors, $K^F_C$. Of course, a production ban is not socially harmful in all scenarios. In particular, if socially responsible investors do not have enough capital or if their investment mandate does not satisfy Conditions 1 and 2, they are unable to steer the entrepreneur towards the socially efficient choice. In this case, production bans can increase welfare as they may prevent the adoption of the dirty technology by firms that are not disciplined by socially responsible investors.

**Pigouvian taxes.** Now suppose that the regulator imposes a tax on the social cost generated by the firm’s production (e.g., a tax assessed on the firm’s carbon emissions), resulting in a total tax of $\phi\tau K$ for a firm producing with technology $\tau$ at scale $K$. Set appropriately, such a tax can make dirty production financially nonviable. While
this prevents dirty production, it reduces or eliminates the threat of dirty production, resulting in similar effects to a production ban. However, welfare can be even lower than under a production ban, because the firm is taxed also on the clean technology, by an amount $\phi C K$, lowering the maximum feasible scale of clean production below $K_C^F$.

4.3 Impact through Risk Premia

Our framework features universal risk neutrality. As shown, under this assumption a narrow mandate (i.e., the exclusion of polluting stocks by socially responsible investors) has no effect in the presence of competitive financial capital. If financial investors were risk averse, then such exclusion would have an effect that works indirectly through the price of risk. In particular, equilibrium prices would feature differential risk premia for clean and polluting stocks (see, e.g., Heinkel et al., 2001, Pastor et al., 2019, Pedersen et al., 2019). The mechanism for the differential pricing of risk is that the overweighting of clean stocks by socially responsible requires underweighting of clean stocks by financial investors, and, hence, generates imperfect risk sharing. However, Heinkel et al. (2001) conclude that repricing due to imperfect risk sharing may quantitatively be too small to generate impact.\footnote{The size of the effect depends on the wealth share of socially responsible investors and the correlation structure of stocks. Intuitively, if all stocks were perfectly correlated, then exclusion has no effects even in a setting with risk aversion since overweighting polluting stocks does not affect diversification.}

Moreover, even if narrow exclusion generates a modest amount of impact under risk aversion, our analysis shows that this is typically not the optimal mechanism to achieve impact. For example, if a polluting firm produces safe cash flows, then exclusion will not affect the firm's cost of funding and, hence cannot generate impact. In contrast, an increase in clean scale (in the presence of financing constraints) or a direct transfer could achieve impact.
5 Conclusion

A key question in today’s investment environment is to understand conditions under which socially responsible investors can achieve impact. For example, can investors with social concerns influence firms to tilt their production technologies towards lower carbon emissions? To shed light on this question, this paper develops a parsimonious theoretical framework, based on the interaction of production externalities and corporate financing constraints.

Our analysis uncovers the necessity of a broad mandate for socially responsible investors. Given the abundance of competitive financial capital chasing (financially) profitable investment opportunities, it is not enough for socially responsible investors to internalize the social costs generated by the firms they have invested in. Rather, their concern for social costs must be unconditional—indeed independent of their own investment. This condition generates both normative and positive implications. From a positive perspective, our model implies that if current ESG funds lack such a broad mandate, they cannot have impact. From a normative perspective, it states that, if, as a society, we want responsible investors to have impact, their mandate needs to be broad. Moreover, because a broad mandate entails the sacrifice of financial returns, socially responsible funds need to be evaluated according to broader measures, explicitly accounting for real impact rather than focusing solely on financial metrics.

To achieve impact in the most efficient way, it is optimal for socially responsible investors to relax firm financing constraints for clean production, thereby enabling a scale increase of clean technology relative to what financial capital is willing to offer. Doing so generates a complementarity between financial and socially responsible capital, in that welfare is generally highest in an economy in which there is a balance between financial and socially responsible capital.

From a practical investment perspective, our model implies a micro-founded investment criterion for scarce socially responsible capital, the social profitability index (SPI),
which summarizes the interaction of environmental, social and governance (ESG) aspects. Importantly, in line with the broad mandate, the SPI accounts for social costs that would have occurred in the absence of engagement by socially responsible investors. Accordingly, it can be optimal to invest in firms that generate relatively low social returns (e.g., a firm with significant carbon emissions), provided that the potential increase in social costs, if only financially-driven investors were to invest, is sufficiently large. This contrasts with many common ESG metrics that focus on firms’ social status quo.

To highlight these basic ideas, our model abstracts away from some realistic features. These could be analyzed in future work. For example, our model considers a static framework, where investment is best interpreted as new “greenfield” investment. In a dynamic model, other interesting aspects could be studied, namely how to account for (dirty) legacy assets and how to ensure the timely adoption of novel (and cleaner) production technologies as they arrive over time. Because the adoption of future green technologies may be hard to contract on ex ante, such a theory might yield interesting implications on the issue of control. Second, in our analysis, we excluded the possibility that firms may interact (e.g., as part of a supply chain or as competitors). However, it is plausible that the financing of a green technology by one firm may impact other firms (e.g., through cross-firm externalities related to production technologies or by alleviating or worsening financing constraints). While such spillovers are beyond the scope of this paper, they would be interesting to study in follow-up work.
A Proofs

Proof of Lemma 1. The Proof of Lemma 1 follows immediately from the proof of Proposition 1 given below. First, set $\gamma^{SR} = 0$ (so that socially responsible investors have the same preferences as financial investors). Second, to obtain the competitive financing arrangement (i.e., the agreement that maximizes the utility of the entrepreneur subject to the investors’ participation constraint) one needs to choose the utility level of the entrepreneur $u$ in (A.10) such that $\hat{v}_\tau K_\tau(u) - u = 0$.\textsuperscript{27}

Proof of Proposition 1. The Proof of Proposition 1 will make use of Lemmas A.1 to A.5.

Lemma A.1 In any solution to Problem 1, the IR constraint of financial investors, $p X^F - I^F \geq 0$ must bind,

\[ p X^F - I^F = 0. \tag{A.1} \]

Proof: The proof is by contradiction. Suppose there was an optimal contract for which $p X^F - I^F > 0$. Then, one could increase $X^{SR}$ while lowering $X^F$ by the same amount (until (A.1) holds). This perturbation strictly increases the objective function of socially responsible investors in (8), satisfies by construction the IR constraint of financial investors, whereas all other constraints are unaffected since $X = X^{SR} + X^F$ is unchanged. Hence, we found a feasible contract that increases the utility of socially responsible investors, which contradicts that the original contract was optimal. \hfill \blacksquare

Lemma A.2 There exists an optimal financing arrangement with $I^F = X^F = 0$.

Proof: Take an optimal contract $(I^F, I^{SR}, X^{SR}, X^F, K, c, \tau)$ with $I^F \neq 0$. Now consider the following “tilde” perturbation of the contract (leaving $K, c$ and $\tau$ unchanged). Set $\tilde{X}^F$ and $\tilde{I}^F$ to 0 and set $\tilde{I}^{SR} = I^{SR} + I^F$ and $\tilde{X}^{SR} = X^{SR} + X^F$. The objective of socially

\textsuperscript{27}Note that $\hat{v}_\tau = \pi_\tau - \gamma^E \phi_\tau$ in the special case when $\gamma^{SR} = 0$. 

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responsible investors in (8) is unaffected since

\[
p\tilde{X}^{SR} - \tilde{I}^{SR} - \gamma^{SR} \phi_{\tau} K = pX^{SR} - I^{SR} + p\tilde{X}^{F} - \underbrace{I^{F}}_{0} - \gamma^{SR} \phi_{\tau} K
\]

\[
= pX^{SR} - I^{SR} - \gamma^{SR} \phi_{\tau} K, \quad \text{(A.2)}
\]

where the second line follows from Lemma A.1. All other constraints are unaffected since \(\tilde{X}^{F} + \tilde{X}^{SR} = X^{F} + X^{SR}\) and \(\tilde{I}^{F} + \tilde{I}^{SR} = I^{F} + I^{SR}\) □

Lemma A.2 implies that we can phrase Problem 1 in terms of total investment \(I\) and total repayment to investors \(X\) in order to determine the optimal consumption \(c\), technology \(\tau\), and scale \(K\). However, to make the proof most instructive, it is useful to replace \(X\) and \(I\) as control variables and instead use the expected repayment to investors \(\Xi\) and expected utility provided to the entrepreneur \(u\), which satisfy

\[
\Xi := pX, \quad \text{(A.4)}
\]

\[
u := (pR - k_{\tau} - \gamma^{E} \phi_{\tau}) K + I - pX. \quad \text{(A.5)}
\]

Then, using the definition \(\hat{v}_{\tau} := \pi_{\tau} - (\gamma^{E} + \gamma^{SR}) \phi_{\tau} \geq v_{\tau}\), we can write Problem 1 as:

**Problem 2**

\[
\max_{\tau} \max_{u \geq c^{k}} \max_{K, \Xi} \hat{v}_{\tau} K - u \quad \text{(A.6)}
\]

subject to

\[
K \geq 0 \quad \text{(A.7)}
\]

\[
\Xi \leq (pR - \xi) K \quad \text{(IC)}
\]

\[
\Xi \geq -(A + u) + (pR - \gamma^{E} \phi_{\tau}) K \quad \text{(LL)}
\]

Here, the last constraint (LL) can be interpreted as a limited liability constraint,
since it refers to the constraint that upfront consumption is weakly greater than zero (using the aggregate resource constraint in (2)). As the problem formulation suggests, it is useful to sequentially solve the optimization in 3 steps to exploit the fact that $\Xi$ only enters the linear program via the constraints (IC) and (LL), but not the objective (A.6).

As is obvious from Problem 2, only a technology that delivers positive surplus to investors and the entrepreneur (i.e., $\hat{v}_\tau > 0$) is a relevant candidate for the equilibrium technology.\(^{28}\) Now consider the inner problem, i.e., for a fixed technology $\tau$ with $\hat{v}_\tau > 0$ and a fixed utility $u \geq \bar{U}^E$ we solve for the optimal vector $(K, \Xi)$ as a function of $\tau$ and $u$.

\textbf{Lemma A.3} For any $\tau$ with $\hat{v}_\tau > 0$ and $u \geq \bar{U}^E$, the solution to the inner problem, i.e.,

$$\max_{K,\Xi} \hat{v}_\tau K - u \text{ subject to (A.7), (IC) and (LL)}$$

implies maximal scale, i.e.,

$$K_\tau (u) = \frac{A + u}{\xi - \gamma^E \phi_\tau} > 0. \quad (A.8)$$

The expected payment to investors is:

$$\Xi_\tau (u) = (pR - \xi) K_\tau (u). \quad (A.9)$$

\textbf{Proof:} The feasible set for $(K, \Xi)$ as implied by the three constraints (A.7), (IC) and (LL) forms a polygon (see orange region in Figure 1). The upper bound on $\Xi$ in (IC) is an affine function of $K$ through the origin (i.e., linear in $K$) whereas the lower bound in Equation (LL) is an affine function of $K$ (with negative intercept $-(A + u)$). The slope of the lower bound in Equation (LL) is strictly greater than the slope of the upper

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\(^{28}\) Note that $\hat{v}_C$ is unambiguously positive whereas $\hat{v}_D$ could be negative or positive depending on whether the sum $\gamma^E + \gamma^{SR}$ is sufficiently close to 1.
bound in Equation (IC) since

\[
(pR - \gamma^E \phi_T) - (pR - \xi) = \xi - \gamma^E \phi_T \\
> \pi_T - \gamma^E \phi_T \\
> \pi_T - (\gamma^E + \gamma^{SR}) \phi_T = \hat{v}_T > 0,
\]

where the second line follows from the finite scale that is implied by Assumption 1 (i.e., \(\xi > \pi_T\)). Therefore, the intersection of the upper bound (IC) and the lower bound in (LL) defines the maximal feasible scale of \(K\). Choosing the maximal scale \(K_T(u)\) is optimal, since for any given \(T\) with \(\hat{v}_T > 0\) and any fixed \(u \geq \bar{U}^E\), the objective function \(\hat{v}_T K - u\) is strictly increasing in \(K\) and independent of \(\Xi\). The expression for \(K_T(u)\) in Equation (A.8) is obtained from \((pR - \xi) K = -(A + u) + (pR - \gamma^E \phi_T) K\).

Given the solution to the inner problem, \((K_T(u), \Xi_T(u))\), we now turn to the optimal choice of \(u\) which maximizes \(\hat{v}_T K_T(u) - u\) subject to \(u \geq \bar{U}^E\).
Lemma A.4 In any solution to Problem 2, the entrepreneur obtains her reservation utility \( u = \bar{U}^E \).

**Proof:** It suffices to show that the objective is strictly decreasing in \( u \). Using \( K_\tau (u) = \frac{A+u}{\xi-\gamma^E \phi_\tau} \) and \( \hat{v}_\tau = \pi_\tau - (\gamma^E + \gamma^{SR}) \phi_\tau \), we obtain that:

\[
\hat{v}_\tau K_\tau (u) - u = \frac{\hat{v}_\tau}{\xi-\gamma^E \phi_\tau} A - \frac{\frac{\xi+\gamma^{SR} \phi_\tau - \pi_\tau}{\xi-\gamma^E \phi_\tau} u}{\xi-\gamma^E \phi_\tau} \tag{A.10}
\]

Since \( \xi > \pi_\tau \) and \( \xi > \gamma^E \phi_\tau \) (both by Assumption 1), both the numerator and the denominator of \( \frac{\xi+\gamma^{SR} \phi_\tau - \pi_\tau}{\xi-\gamma^E \phi_\tau} \) are positive, so that Equation (A.10) is strictly decreasing in \( u \).

Given that \( u = \bar{U}^E \) the optimal payoff to socially responsible investors for a given \( \tau \) is given by:

\[
U^{SR} = \hat{v}_\tau K_\tau (\bar{U}^E) - \bar{U}^E. \tag{A.11}
\]

We now turn to the final step, i.e., the optimal technology choice.

Lemma A.5 The optimal technology choice is given by:

\[
\hat{\tau} = \operatorname{arg\,max}_\tau \frac{\hat{v}_\tau}{\xi-\gamma^E \phi_\tau}. \tag{A.12}
\]

**Proof:** In the relevant case where \( \hat{v}_D > 0 \), we need to compare payoffs in (A.11). The clean technology is chosen if and only if \( \hat{v}_C K_C (\bar{U}^E) > \hat{v}_D K_D (\bar{U}^E) \), which simplifies to (A.12). If \( \hat{v}_D \leq 0 \), then A.12 trivially holds as only \( \hat{v}_C > 0 \).

Lemmas A.3 to A.5, thus, jointly characterize the solution to Problem 2, which, in turn, allows us to retrieve the solution to the original Problem 1. That is, substituting the expression for \( \bar{U}^E \) in Equation (5) into \( \hat{K} = K_{\hat{\tau}} (\bar{U}^E) \) yields Equation (10). Moreover, since \( (LL) \) binds, we obtain that \( \hat{c} = 0 \). The aggregate resource constraint in (2) then implies that total investment by both investors must satisfy \( \hat{I} = \hat{K} k_{\hat{\tau}} - A \), whereas \( (IC) \) implies that \( \hat{X} = \left( R - \frac{B}{\Delta p} \right) \hat{K} \). Since any agreement must satisfy \( X^F + X^{SR} = \hat{X} \) and
\( I^F + I^{SR} = \hat{I} \), we can trace out all possible agreements using the fact that financial investors break even (Lemma A.1), meaning that \( pX^F - I^F = 0 \) and \( X^F \in [0, R] \).

**Proof of Proposition 2.** See discussion in main text.

**Proof of Proposition 3.** See discussion in main text.

**Proof of Proposition 4.** The social profitability index is defined as:

\[
SPI = \frac{\Delta U^{SR}}{I^{SR}} \tag{A.13}
\]

Using Proposition 1, we obtain that the minimum investment that is sufficient to induce a change in production technology is given by

\[
I_{\text{min}}^{SR} = (\xi - \pi_C) \hat{K} - A. \tag{A.14}
\]

The corresponding (maximal) SPI is, hence, given by

\[
SPI_{\text{max}} = \gamma^{SR} \frac{\Delta\phi}{\Delta \pi - \frac{\gamma_E}{\xi} (\Delta\phi (\xi - \pi_C) + \Delta \pi \phi_C)} - 1 \tag{A.15}
\]

which is increasing in \( \Delta\phi, \xi, \) and \( \gamma^E \) and decreasing in \( \Delta \pi \).
References


